

# Modeling of WDM systems in Highly and Weakly Dispersive Nonlinear Regimes



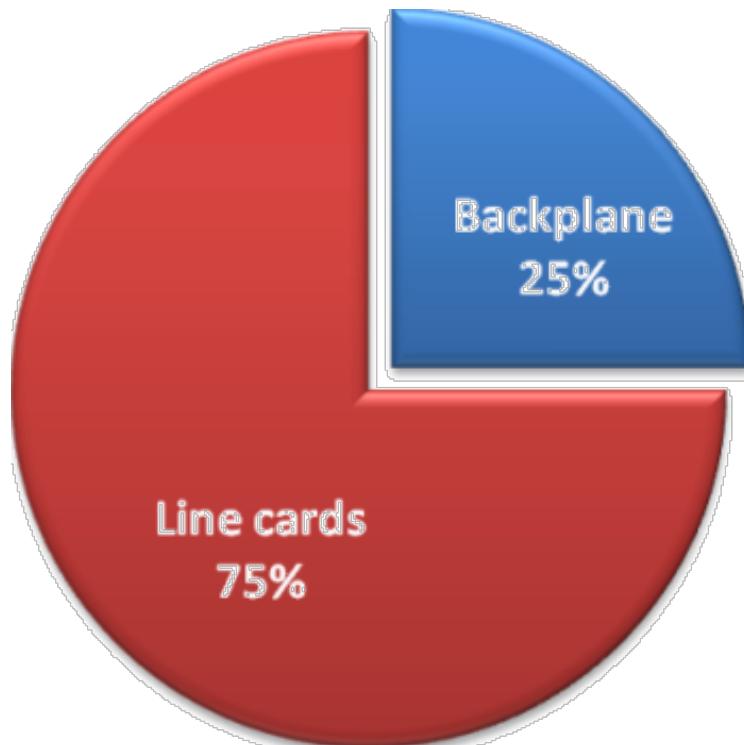
Francesco Matera  
Fondazione Ugo Bordoni  
[mat@fub.it](mailto:mat@fub.it)

# Outline

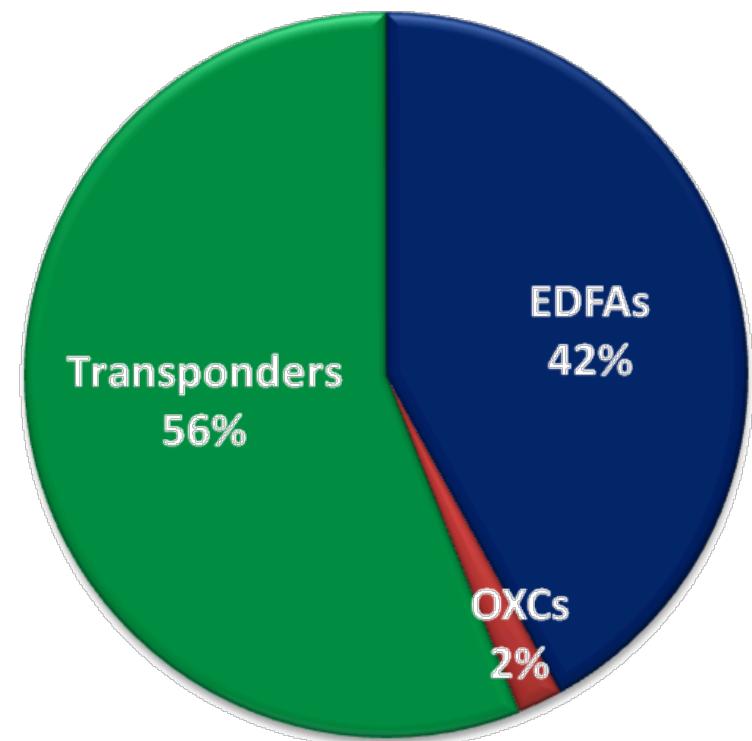
- For network design simple methods to evaluate system performance are necessary taking into account Kerr effect (ITU-T SG15 G.680). The energy saving topic!
- Performance evaluation models in highly dispersive regime
- Importance of Gaussian models
- Here a simple Q factor theoretical approach is adopted for mixed line rate WDM systems, tested with simulations

# Power Consumption in Core Networks

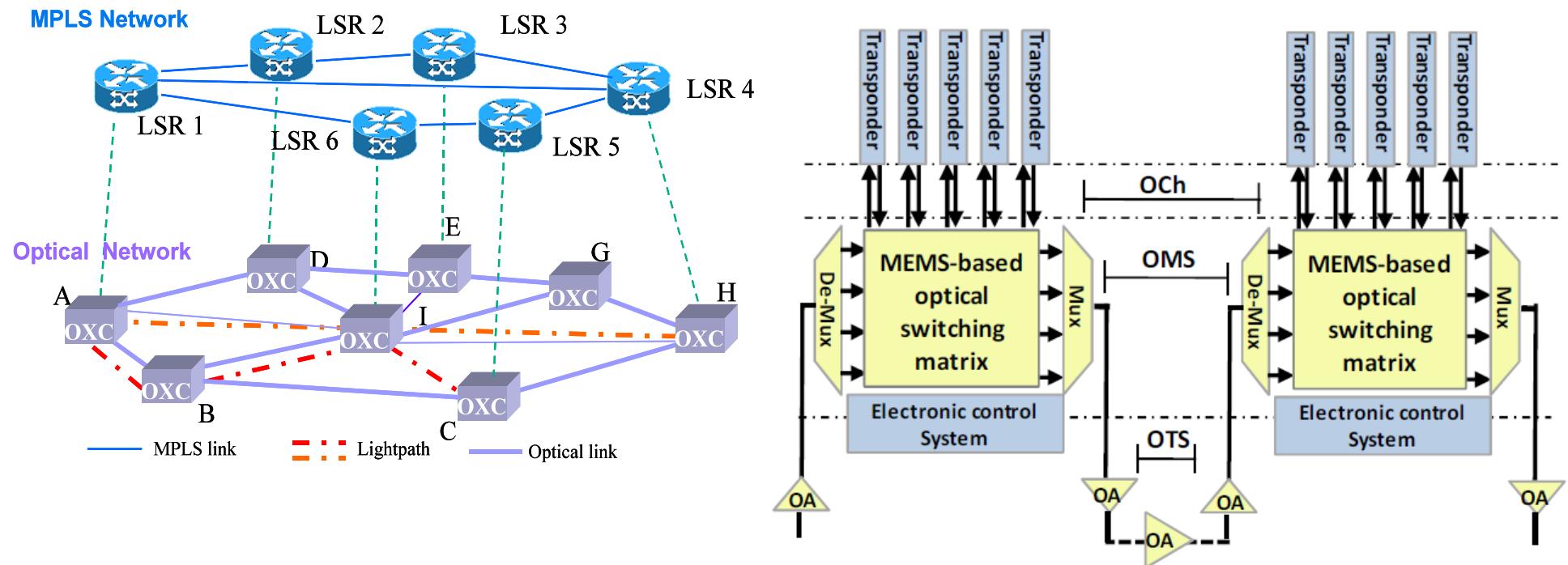
IP network layer



WDM network layer

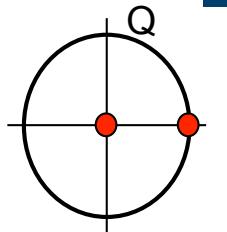


# Network Model



Routing vs Optical paths?

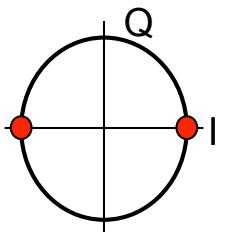
# Modulation formats



IM-DD



- 😊 Sistema consolidato
- 😊 Semplici TX e RX
- 😢 Forti limitazioni a sostenere bit rate elevati

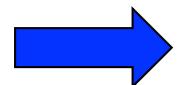


PSK

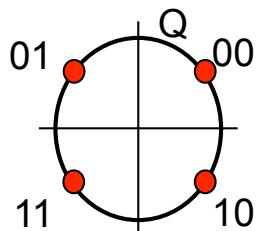


- 😊 Limite quantico si riduce a 18 fotoni/bit e 3 dB in più
- 😢 Ricezione coerente con PLL ottico

DPSK



- 😊 Non necessita di rivelazione coerente
- 😢 Aumenta la complessità del TX e RX rispetto L'IM-DD



QPSK



- 😊 Efficienza spettrale doppia → tolleranza alla CD e PMD
- 😢 Ricezione coerente con PLL ottico

DQPSK



- 😊 Efficienza spettrale doppia
- 😊 Non necessita di rivelazione coerente
- 😢 Aumenta la complessità del TX e RX rispetto al DPSK

# WDM systems



- Nx100 Gb/s, mx400 Gb/s
- Managed dispersion compensation (in-line) vs unmanaged dispersion compensation (all at the End)
- Coherent detection (100 Gb/s Polmux-QPSP)
- Mixed line rate

$$Q = \frac{\langle \Im_1 \rangle - \langle \Im_0 \rangle}{\sigma_1 + \sigma_0}$$

# Theoretical Overview: Highly Dispersive Regime (HDR)

- Gaussian Noise model for WDM

Poggiolini, J. Lightwave Technol. **31** 446 (2013).
- Single-channel Time domain approach

Mecozzi, Matera, Settembre, Tabacchiera, Opt. Expr. (2011), sing. Ch.  
Mecozzi Matera, Opt. Lett. **19** 3903 (2011). Polmux
- WDM time-domin approach

Mecozzi, Essiambre, J. L.T (2012) stat. independence of frequencies
- Discrete –Time channel model

Secondini, Forestieri, Prati J. L.T (2013) Modulation format
- Time domain approach: Limits of Gaussian approach

Dar, Feder, Mecozzi,Shtaif, Optics express 2013, stat. dependence of frequencies

# Theory (1): HDR

Matera, ECOC 2013, single channel:

$$Q = \frac{\sqrt{P_{AV}}}{\sqrt{\xi R_b N_{ASE} N + \rho \gamma^2 P_{AV}^3 L_{NLI}^2}}$$

$P_{AV}$  input signal average power,  $N_0 = \hbar \omega_0 (G - 1) n_{sp}$

$R_b$  boud rate,  $\xi$  depends on modulation-detection format

$L_{NLI}$  Nonlinear Interaction Length, obtained by the variance of the photodiode current;  $f$ (pulse duration, loss, GVD, boud time); see:

DQPSK and DPSK: Mecozzi, Matera, Settembre, Tabacchiera, Opt. Expr. (2011).

$N$  Fiber spans,  $\rho$  takes into account Polmux

## Theory (2): HDR

### WDM approach

Mecozzi, Essiambre, J. L.T (2012) stat. independence of frequencies

$$Q = \frac{\sqrt{P_{AV}}}{\sqrt{\xi R_b N_{ASE} N + \rho \gamma^2 P_{AV}^3 L_{NLI}^2 + \frac{4 \gamma^2 P_{Av}^3 L S_B}{|\beta_2| R_b^2}}}$$
$$\sigma_{WDM}^2 = \frac{4 \gamma^2 P_{Av}^3 L S_B}{|\beta_2| R_b^2}$$
$$S_B \approx \frac{\kappa R_b}{\pi \Delta f} [\ln(m/2) + 0.57]$$

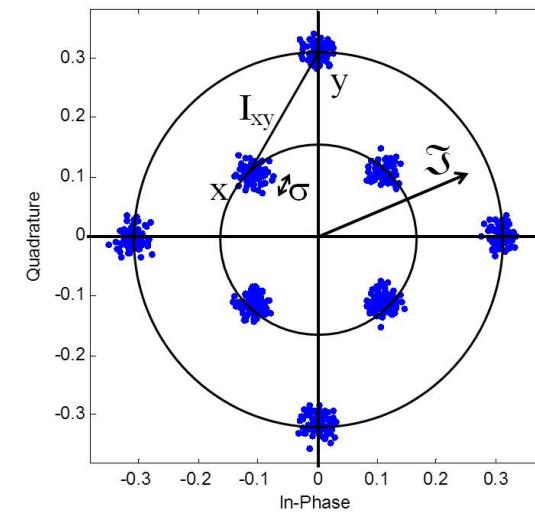
$\Delta f$  frequency spacing;  $\kappa$  depends on modulation ring

Bosco, Poggiolini, Curri, Carena, Fotonica 2013, Milan (IT) May 21-23, 2013

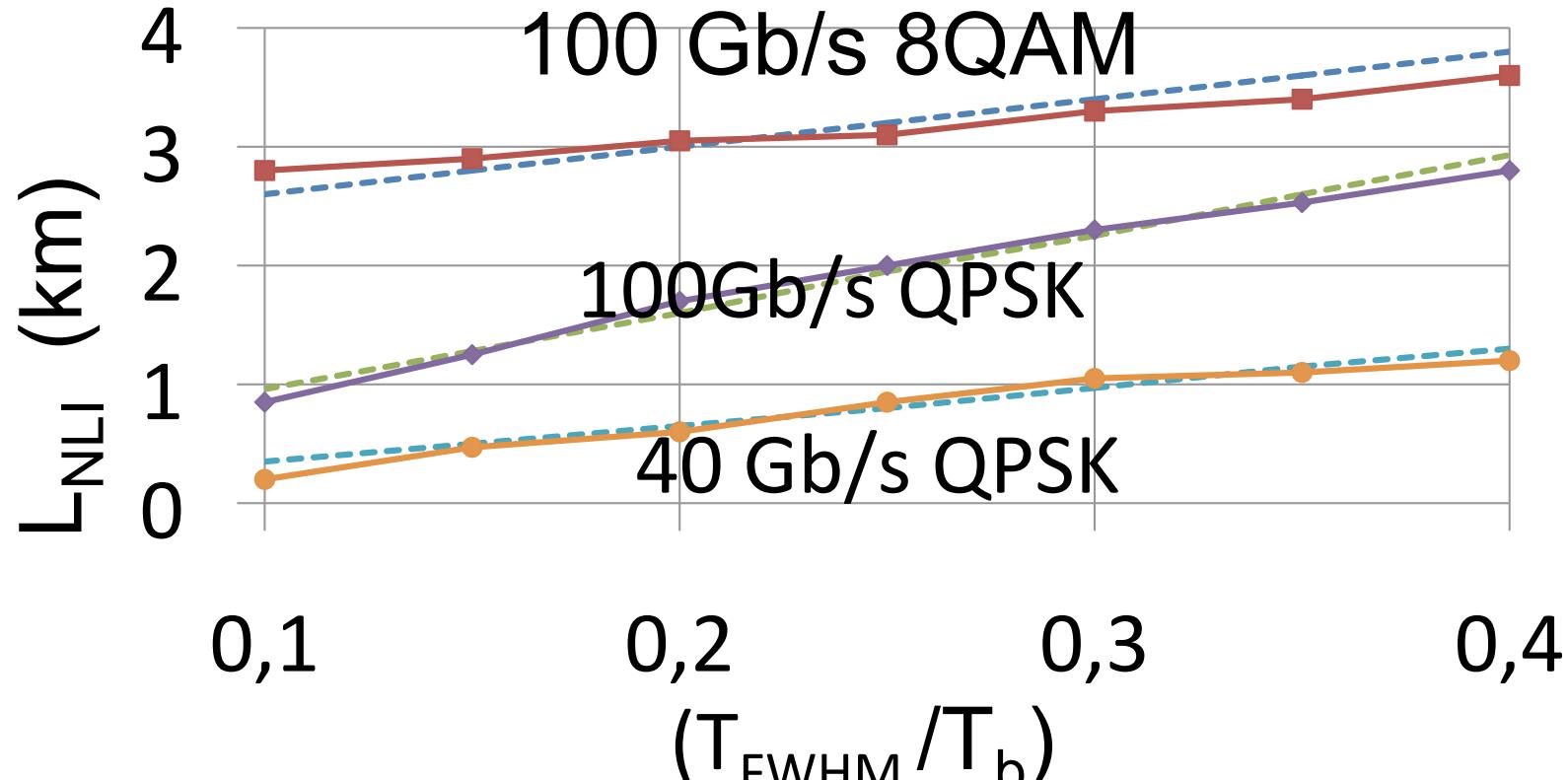
# Simulation model

- Split-step method
- IM-DD, DPSK, DQPSK, QPSK, 8QAM
- Polarization multiplexing
- 4096 symbols

$\gamma=1.3 \text{ W}^{-1}\text{km}^{-1}$ , GVD=16 ps/nm/km,  
loss=0.25 dB km, Lamp=100 km



# Nonlinear Interaction Length



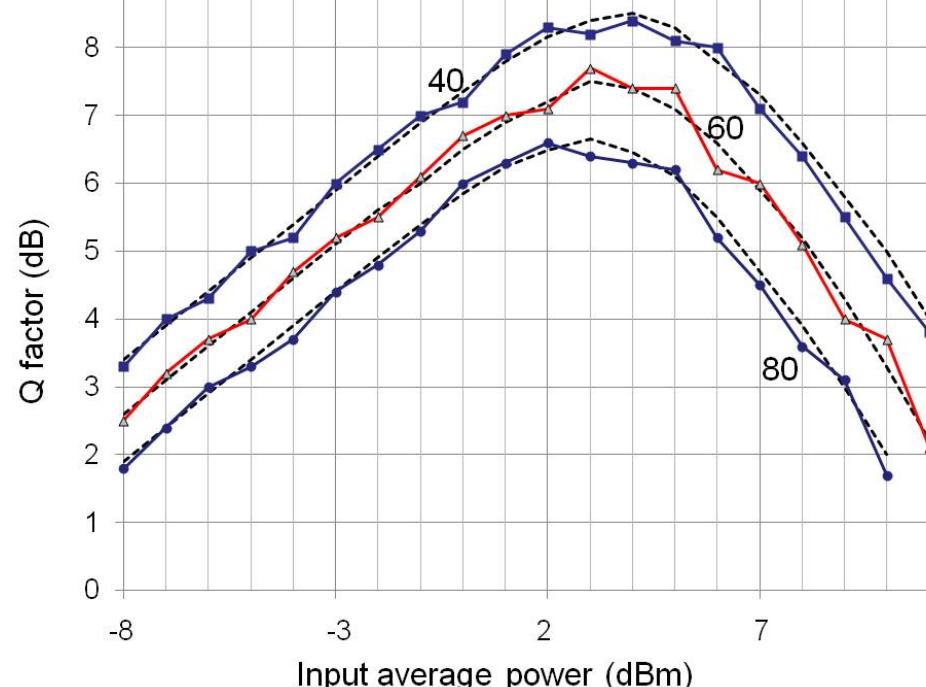
$L_{NLI}$  N for in-line compensation

$N^\Gamma$  for compensation all at the end,  $0.5 < \Gamma < 1$

# Weakly dispersive regime?

$L_{NLI}$  : theoretical calculation does not coincide with simulations but still valid 1/P Q factor behavior

$L_{NLI}^*$  estimated by simulation



10 Gb/s IM-DD system in a link composed by N (40, 60, 80), G.652 fibres. The chromatic dispersion is compensated at each span output. Dashed lines theoretical Q factor , solid lines simulations.

# General Q factor evaluation for Mixed line Rate

Channels statistically independent

$$\sigma_{WDM}^2 = \sum_i \frac{4\gamma^2 P_{Avi}^3 L_A N_i S_{Bi}}{|\beta_2| R_{bi}^2} \quad S_{Bi}^2 = \kappa_i \frac{1}{2\pi T \Delta f_i}$$

$L_{NLI}$  is evaluated theoretically in highly dispersive regime, estimated by simulations for weakly dispersive (10 Gb/s)

## For exact evaluation...

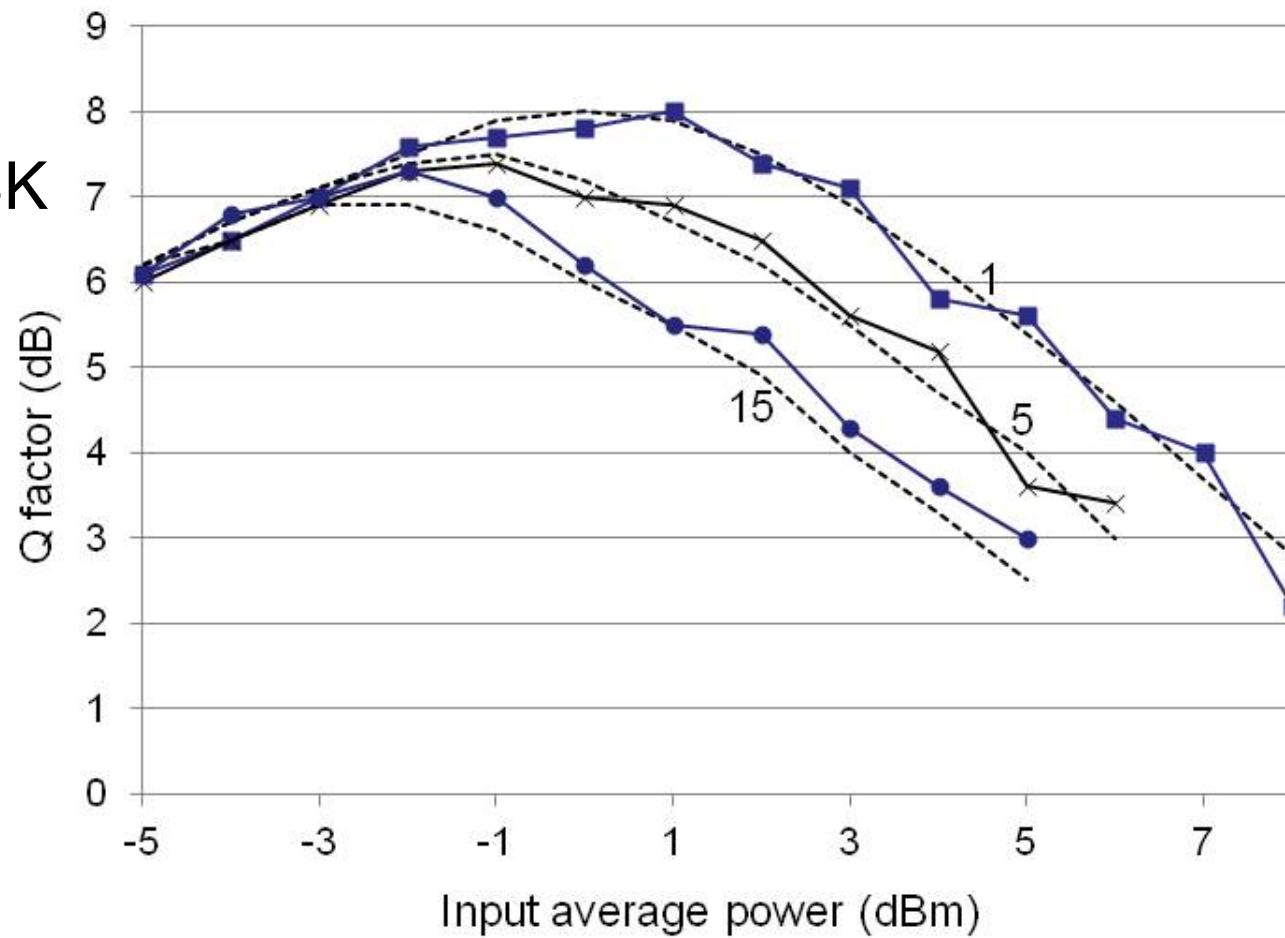
- To take into account all the SPM and XPM effects the Mecozzi model can be adopted and you may evaluate your system performance at

<http://nlinwizard.eng.tau.ac.il>

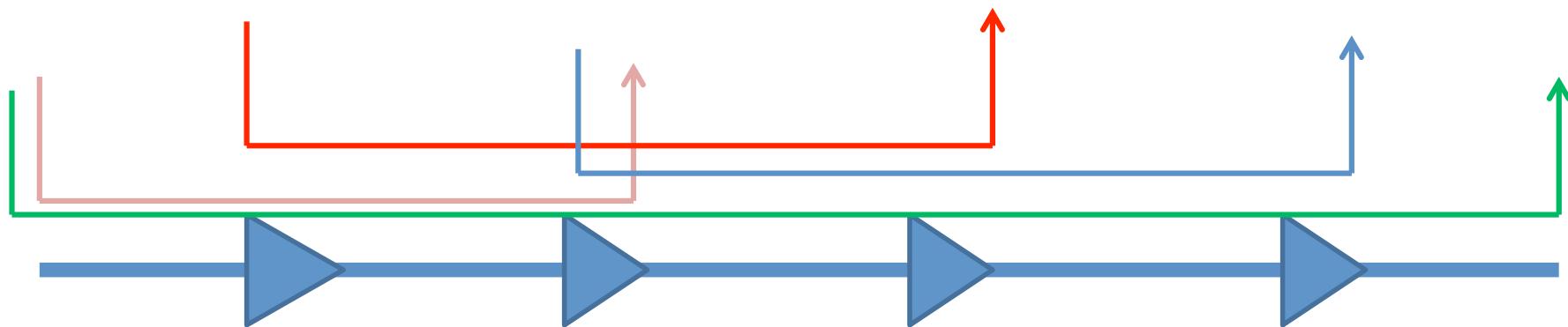
Dar, Feder, Mecozzi, Shtaif, Optics express 2013, stat. dependence of frequencies

# WDM FIXED LINE RATE

100 Gb/s DQPSK  
Comp. All at the End

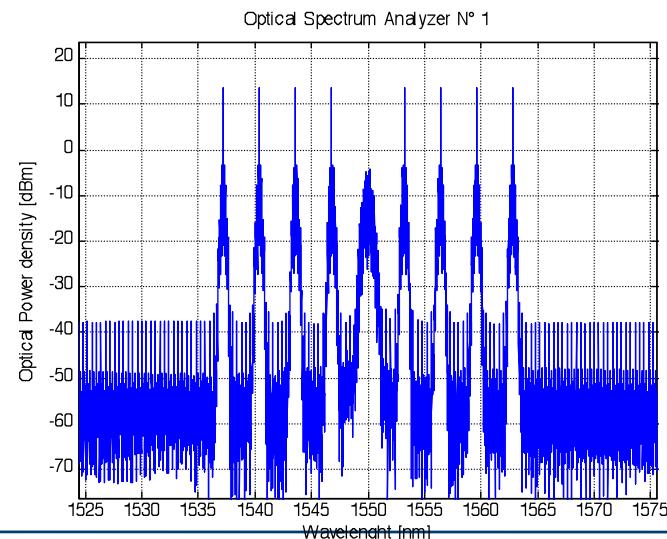


# Link characteristics



## Link parameters

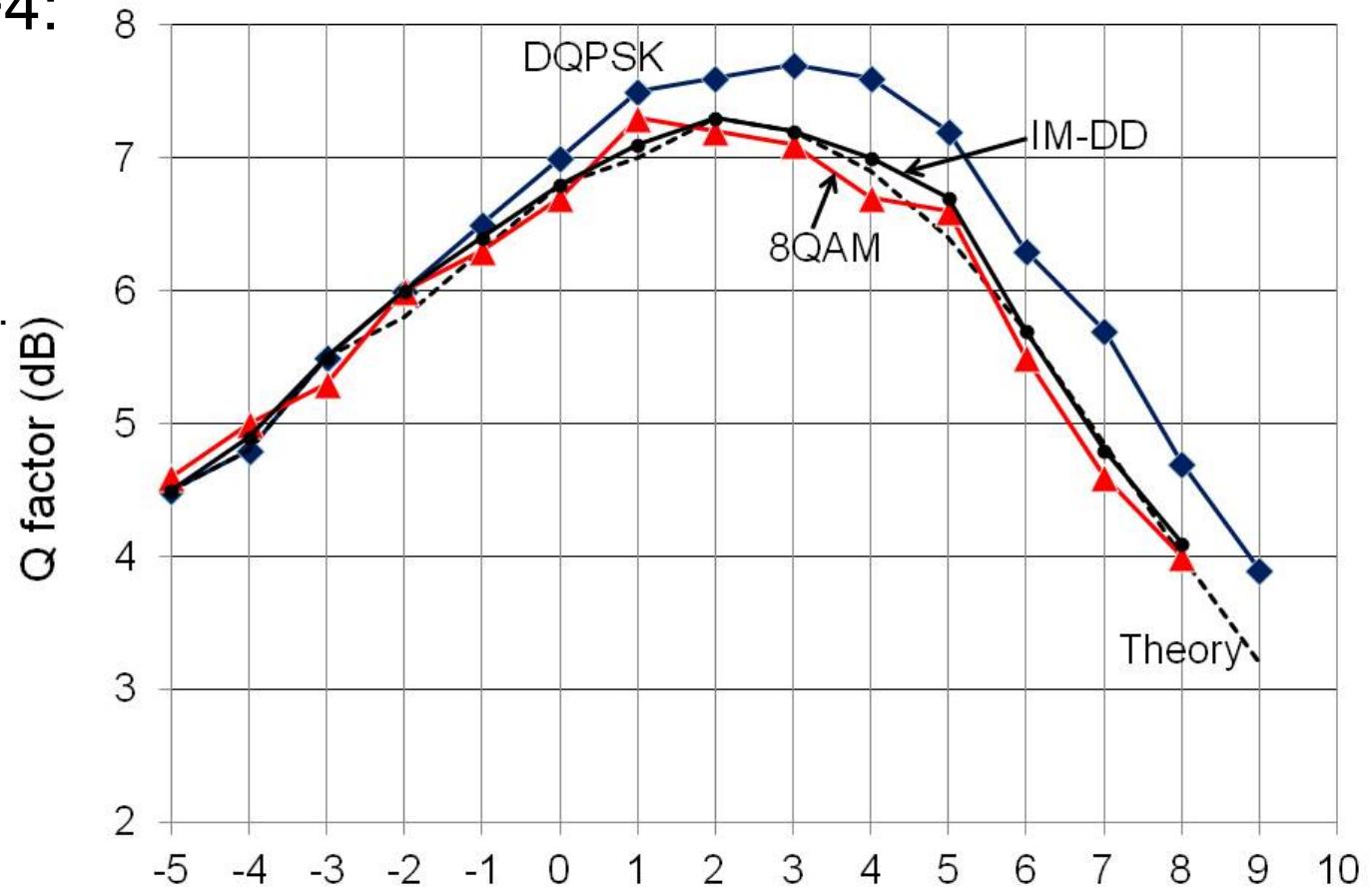
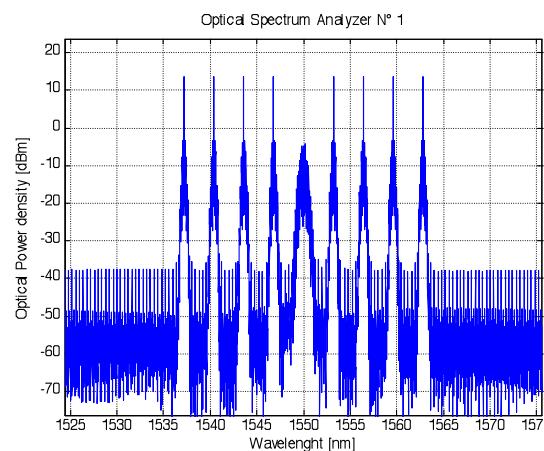
$\gamma=1.3 \text{ W}^{-1}\text{km}^{-1}$ , GVD=16 ps/nm/km,  
loss=0.25 dB km, Lamp=100 km



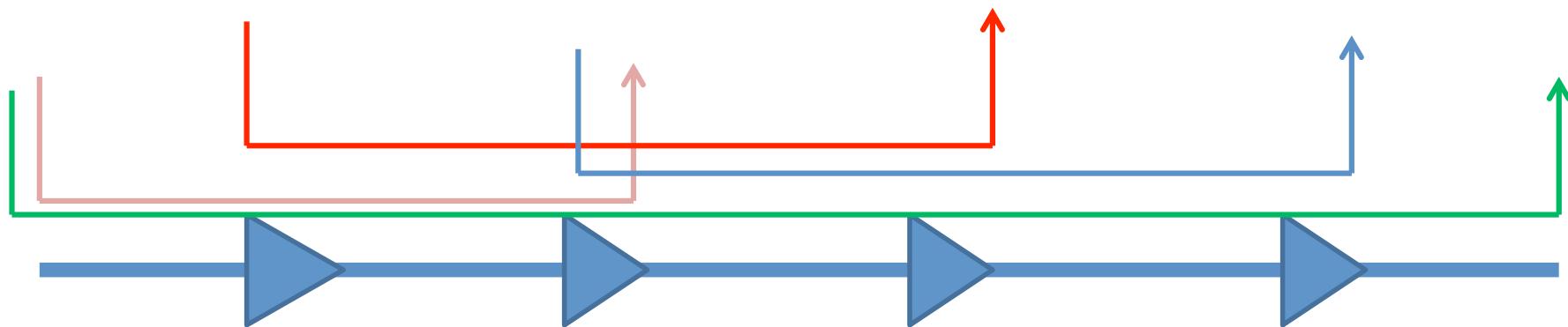
# Mixed Line Rate

100 Gb/s 8QAM +4+4:  
100 Gb/s DQPSK;  
100 Gb/s 8QAM;  
10 Gb/s IM-DD

Compensation *all at the end.*



# Link characteristics



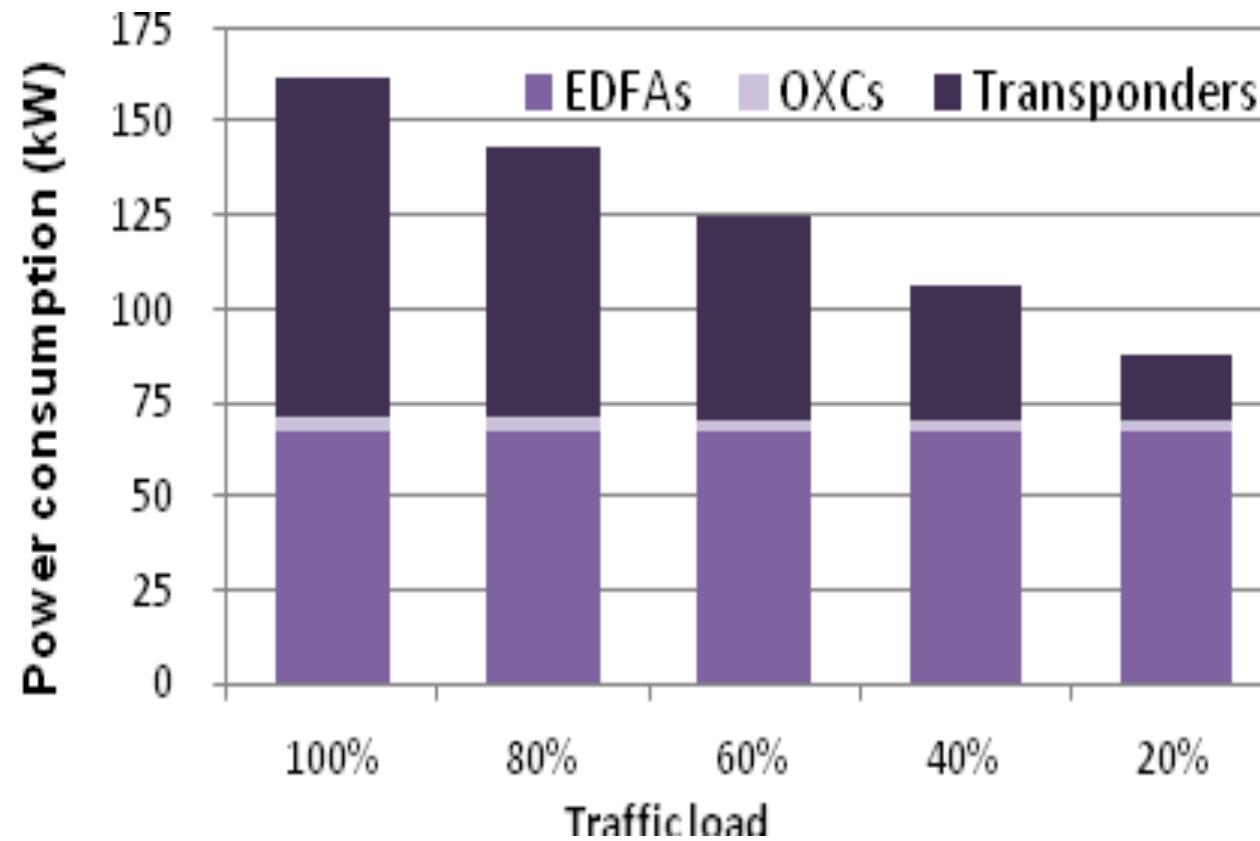
Ideal Add drop, 30 channels, 1000 km  
IM-DD, DQPSK, QPSK, 8QAM; RZ gaussian pulse

$\gamma=1.3 \text{ W}^{-1}\text{km}^{-1}$ , GVD=16 ps/nm/km,  
loss=0.25 dB/km, Lamp=100 km

# WDM link performance

System	$\tau_{FWHM}$ (ps)	$L_{NLI-0}$ (km)	path	$P_{Av}$ (dBm)	Freq. posit.	Qth	Qsim
6x40 Gb/s IM-DD	5	0.96	1-6	2	1,2,3,4 ,5,8	6.3	6.5
9x10 Gb/s IM-DD	25	0.13	1-10	0	6,7,91 0,11 12,13 17,18	6.2	6.8
3x40 Gb/s DPSK	5	0.86	4-10	2	14,15, 16	6.2	6.5
4x100 Gb/s 8QAM	7.5	3.46	3-7	4	19,20 21,22	6.5	6.8
4x100 Gb/s DQPSK	5	2.5	3-9	4	23,24 25,26	6.1	6.6
4x100 Gb/s QPSK	5	2.6	3-10	4	27,28 29,30	6	6.5

# Power Consumption



# Conclusions

- Proposed a simple approximated analytical approach to evaluate the performance of MLR WDM links
- Main limitations for mixed IM-PM systems (some dB)
- Useful for Network design: i.e. Wavelength assign and energy saving
- Further investigation on short links